

# Recursive method tracing

## Stack based approach

### Simple Example

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What does mystery(5) return?

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3;
    else
        return mystery(b - 1) + 2;
}
```

There are 2 recursive calls in mystery. Label the recursive calls 1 & 2.

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

Use a stack to keep track of the method calls and the return values.  
The initial call is `mystery(5)`. Abbreviate the method name as `m`.

`m(5)`

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

$m(5)$  stops at the line labeled Call 2 when it calls  $m(4)$ .

Use a subscript to note the call  $m(5)$  stopped at.

Add the new call to  $m(4)$  to the top of the stack.

$m(4)$

$m(5)_2$

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

$m(4)$  stops at Call 1 and calls  $m(3)$ .

$m(3)$

$m(4)_1$

$m(5)_2$

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

m(2)

m(3)<sub>2</sub>

m(4)<sub>1</sub>

m(5)<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

m(1)  
m(2)<sub>1</sub>  
m(3)<sub>2</sub>  
m(4)<sub>1</sub>  
m(5)<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

m(0)  
m(1)2  
m(2)1  
m(3)2  
m(4)1  
m(5)2

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

~~m(0)~~ returns 0 and terminates.

Cross out the call to ~~m(0)~~ to indicate that the method has terminated.

Write the return value to the right of the method.

~~m(0)~~                    returns 0  
m(1) 2  
m(2) 1  
m(3) 2  
m(4) 1  
m(5) 2

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

Control returns to the topmost non-terminated method on the stack,  $m(1)$ .  
 $m(1)$  was suspended on the line labeled Call 2 when it called  $m(0)$ .  
The call to  $m(0)$  returned 0.  
 $m(1)$  returns  $0 + 2 = 2$ .

$\cancel{m(0)}$	returns 0
$\cancel{m(1)}_2$	returns 2
$m(2)_1$	
$m(3)_2$	
$m(4)_1$	
$m(5)_2$	

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

Control returns to `m(2)` which was suspended on the line labeled Call 1.  
The call to `m(1)` returned 2.  
`m(2)` returns  $2 + 3 = 5$ .

<del><code>m(0)</code></del>	returns 0
<del><code>m(1)</code></del> <sub>2</sub>	returns 2
<del><code>m(2)</code></del> <sub>4</sub>	returns 5
<code>m(3)</code> <sub>2</sub>	
<code>m(4)</code> <sub>1</sub>	
<code>m(5)</code> <sub>2</sub>	

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

<del>m(0)</del>	returns 0
<del>m(1)</del> <sub>2</sub>	returns 2
<del>m(2)</del> <sub>4</sub>	returns 5
<del>m(3)</del> <sub>2</sub>	returns 7
<del>m(4)</del> <sub>1</sub>	
<del>m(5)</del> <sub>2</sub>	

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

<del>m(0)</del>	returns 0
<del>m(1)</del> <sub>2</sub>	returns 2
<del>m(2)</del> <sub>4</sub>	returns 5
<del>m(3)</del> <sub>2</sub>	returns 7
<del>m(4)</del> <sub>4</sub>	returns 10
<del>m(5)</del> <sub>2</sub>	

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

<del>m(0)</del>	returns 0
<del>m(1)</del> <sub>2</sub>	returns 2
<del>m(2)</del> <sub>4</sub>	returns 5
<del>m(3)</del> <sub>2</sub>	returns 7
<del>m(4)</del> <sub>4</sub>	returns 10
<del>m(5)</del> <sub>2</sub>	returns 12

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```